

# ESPI assisted Hole Drilling Method for Residual Stress Measurement

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## Hole Drilling Method

- Measurement of the in-plane strain relaxation produced by hole drilling
- Estimation of the residual stress by evaluating the strain relaxation data
- Incremental drilling and measurement provides an estimate of the variation of stress with depth

## Advantages

Advantages of the ESPI assisted strain relaxation measurement:

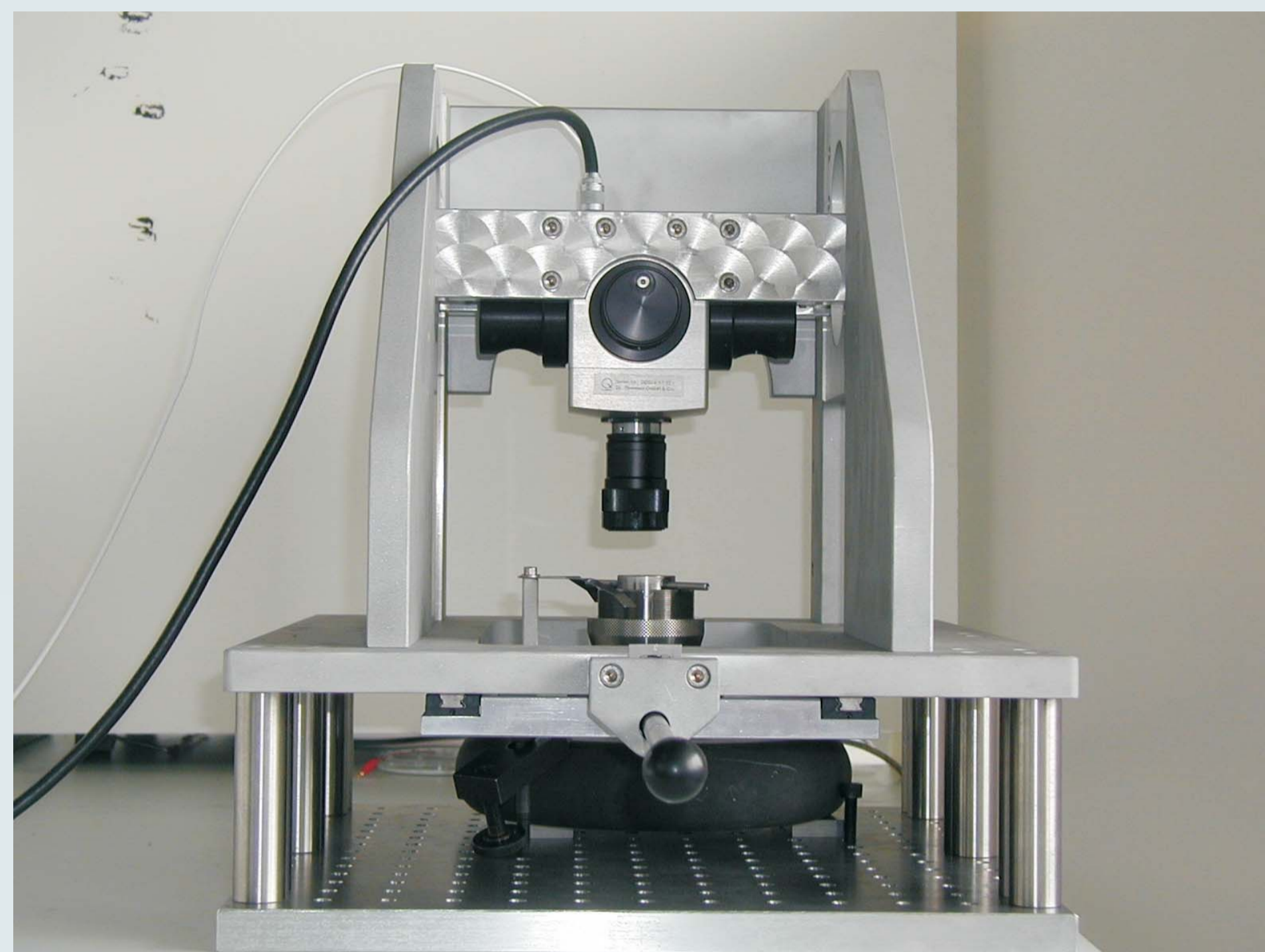
- No surface preparation
- No application of strain gage
- No wiring
- No alignment of the drilling axis
- Non-contact optical measurement
- Increased number of data  
→ noise reduction, enhanced calculation accuracy

## Requirements

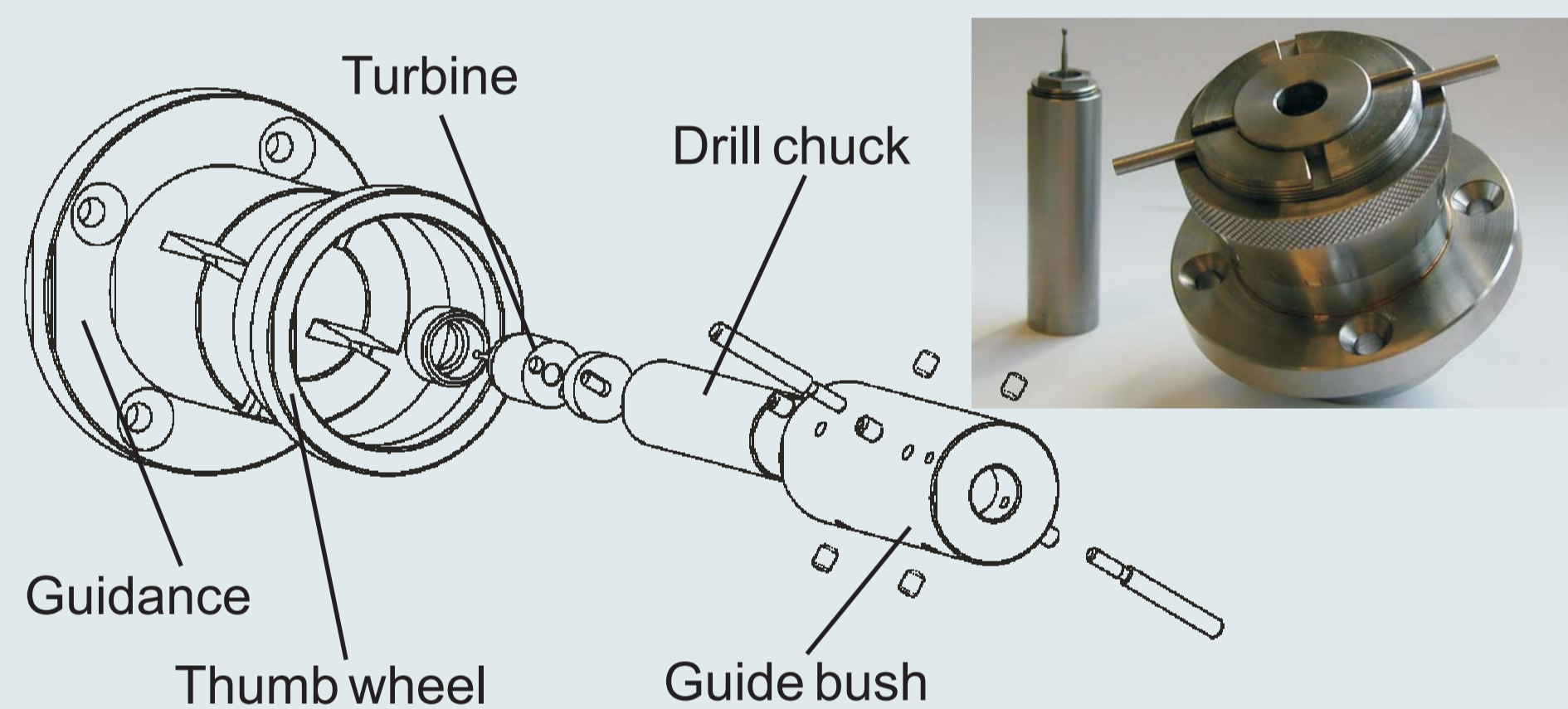
Requirements to the ESPI system:

- highest sensitivity
- measurement field: approx. 20 x 20 mm<sup>2</sup>

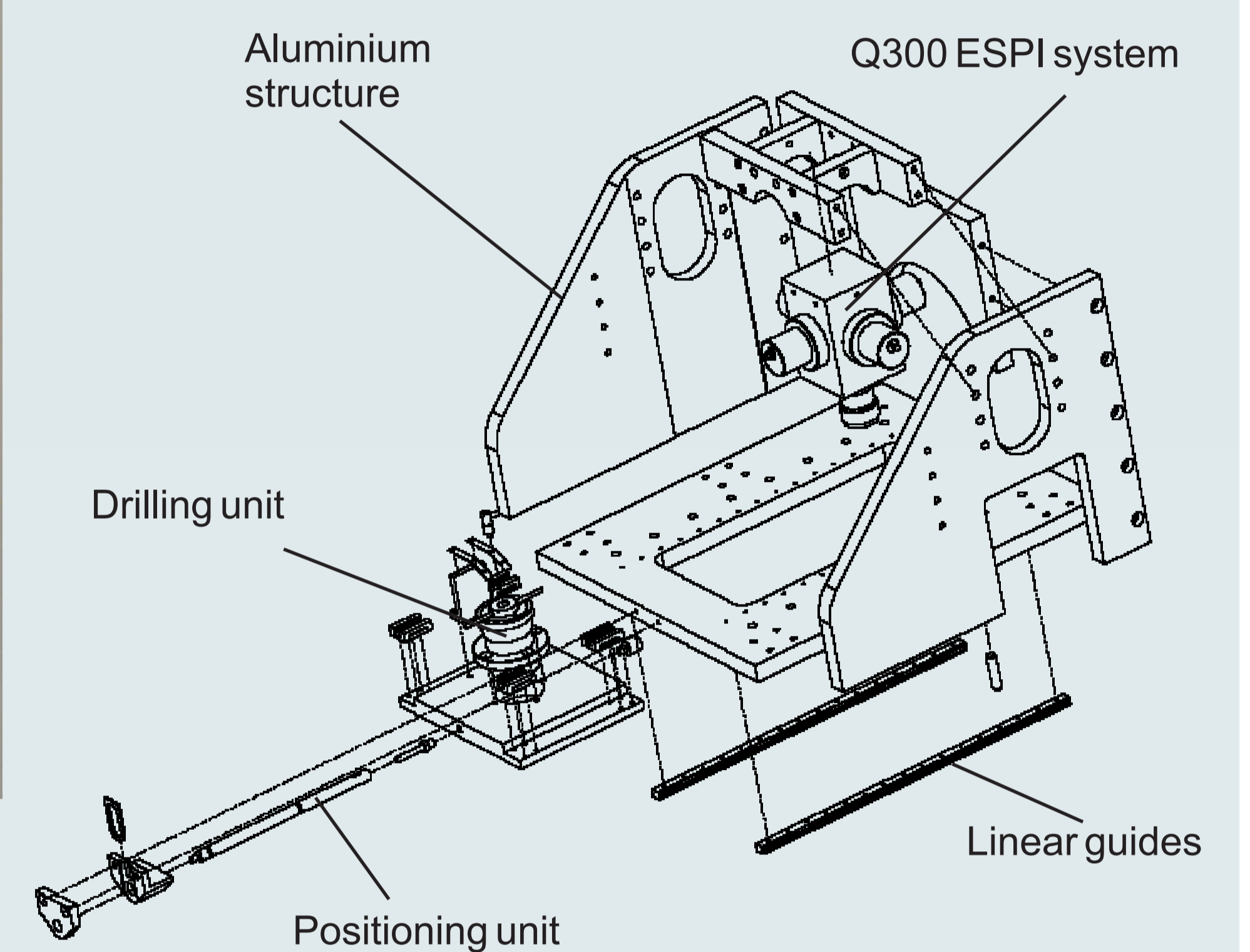
## Experimental Setup



Drilling unit:



### Structure and mechanical devices:



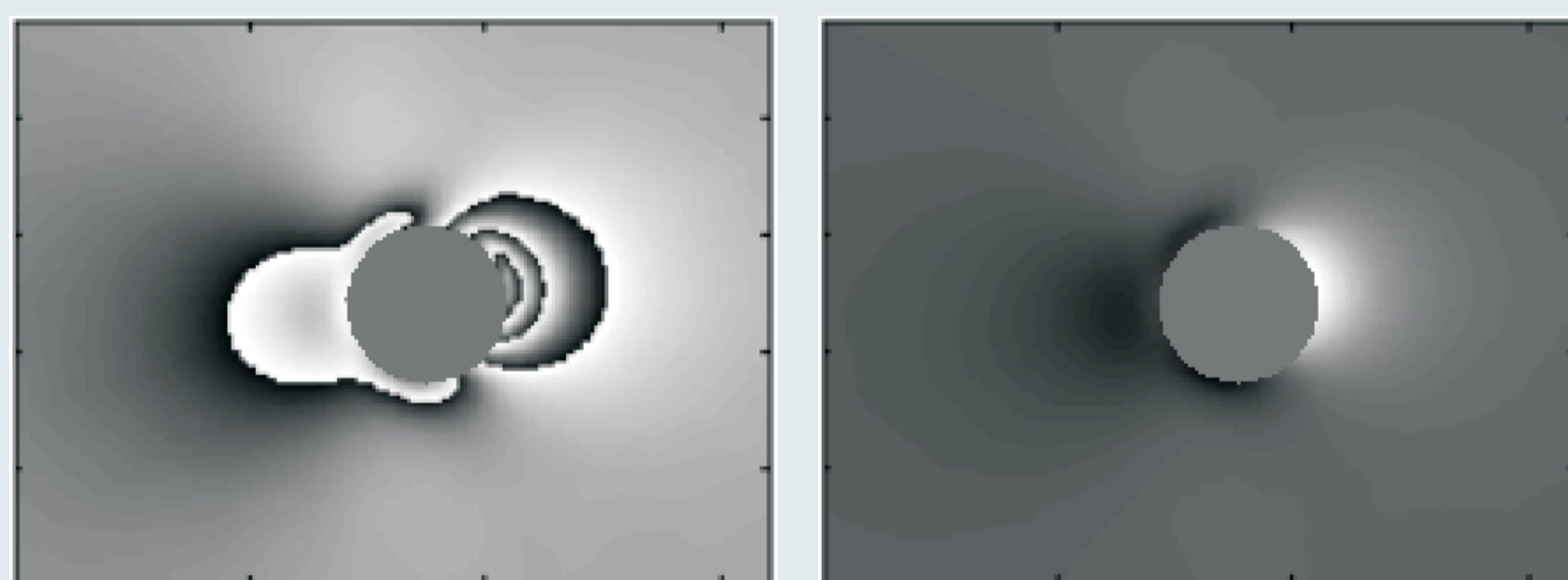
### Characteristics:

- High positioning accuracy of the drilling unit
- High stiffness of the overall structure
- Vertical and horizontal usage possible
- Flexible mounting of the specimen
- Low maintenance
- No electronic devices
- Transportable

## Evaluation of the relaxation data - Solving an inverse problem

### Measurement of the relaxation data

The relaxed inplane deformation around the blind hole is recorded after each drilling step.



Fringe pattern

Radial displacement

The radial displacement component  $u_r$  at a chosen radius  $r_m$  leads to the transformed deformation variables

$$u_p(h) = \frac{1}{2\pi} \int_0^{2\pi} u_r(r_m) d\varphi$$

$$u_q(h) = \frac{1}{2\pi} \int_0^{2\pi} u_r(r_m) \cos(2\varphi) d\varphi$$

$$u_t(h) = \frac{1}{2\pi} \int_0^{2\pi} u_r(r_m) \sin(2\varphi) d\varphi$$

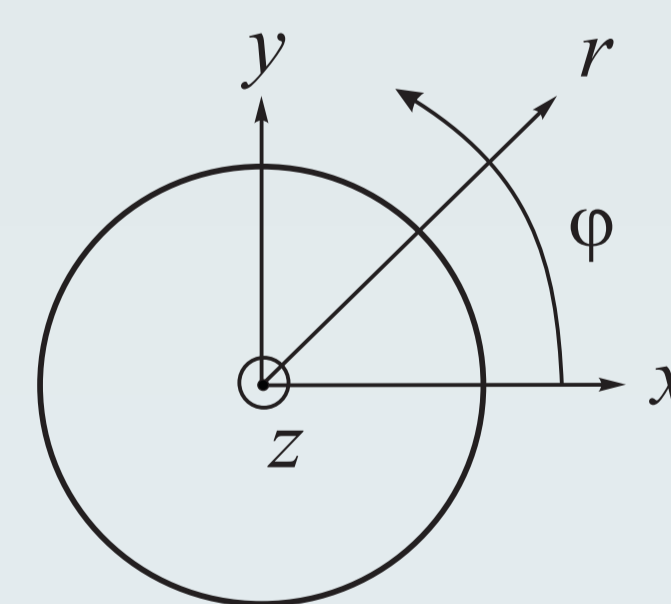
### Estimation of the residual stresses

The stress state is specified by the transformed stress variables:

$$P = \frac{\sigma_x + \sigma_y}{2}$$

$$Q = \frac{\sigma_x - \sigma_y}{2}$$

$$T = \sigma_{xy}$$



Considering a linear elastic constitutive law, the transformed stress variables are associated with the deformation variables by the following integral

$$u_p(h) = \frac{1+\nu}{E} \int_0^h \bar{A}(H, h) P(H) dH$$

$$u_q(h) = \frac{1}{E} \int_0^h \bar{B}(H, h) Q(H) dH$$

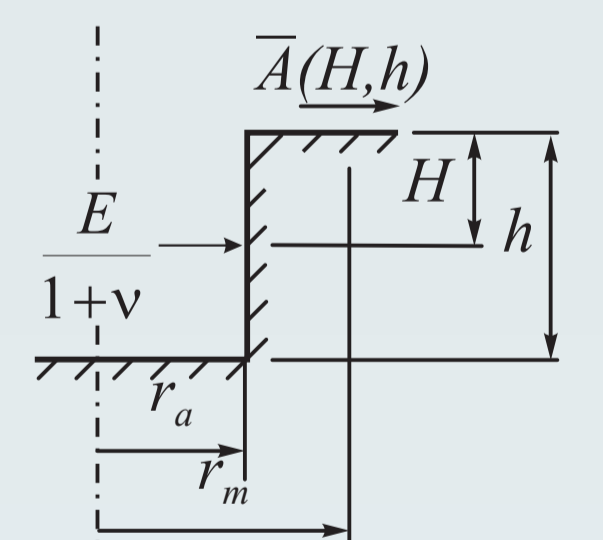
$$u_t(h) = \frac{1}{E} \int_0^h \bar{B}(H, h) T(H) dH$$

Following the concept of the integral method, the discretization of these relationships into finite depth increments leads to a linear system of equations. The displacement relaxation functions  $\bar{A}$  and  $\bar{B}$  can be obtained numerically by FEM analysis.

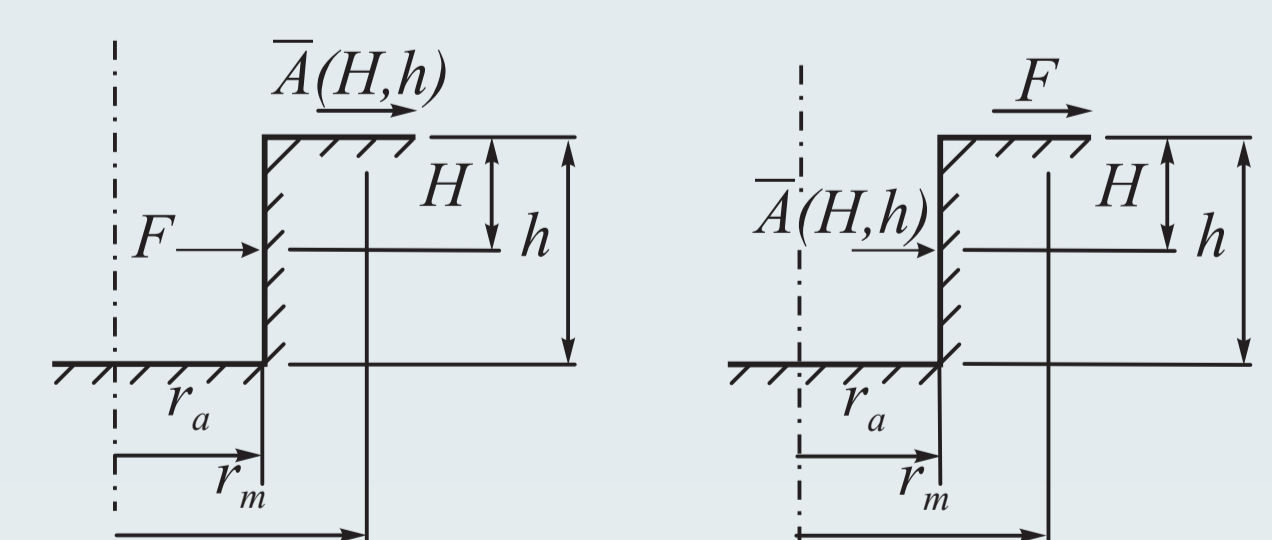
### Calculation of the calibration data

$\bar{A}(H, h)$  can be interpreted as displacement caused by a loading

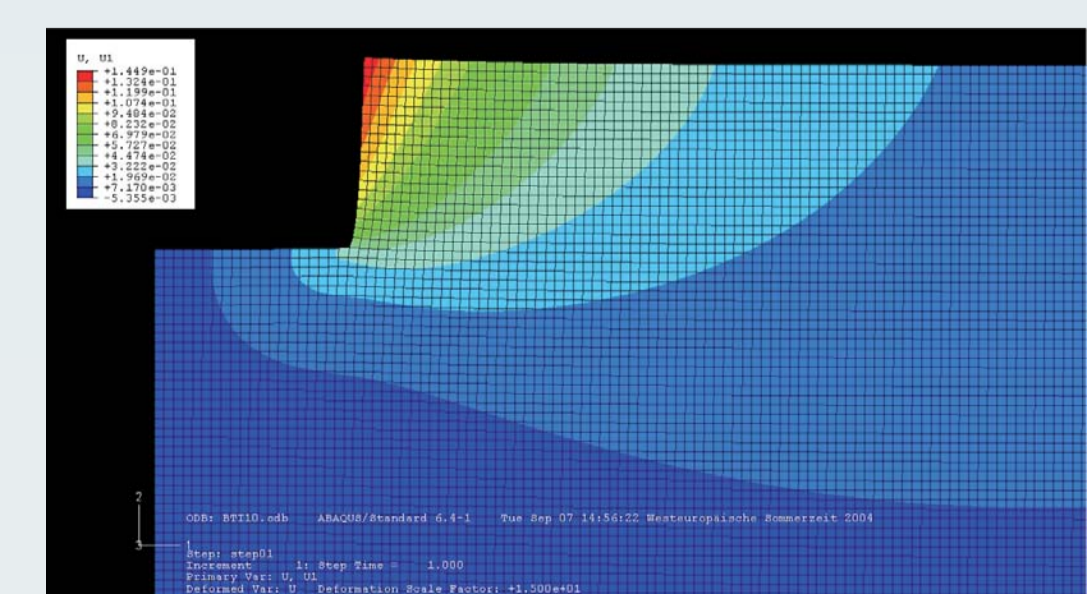
$$p(H) = \frac{E}{1+\nu} \delta(H)$$



Using Maxwells reciprocity theorem the displacement relaxation function for the drilling depth  $h$  can be estimated with a single FEM-analysis.



Application of Maxwells reciprocity theorem



Finite Element Model [radial displacements]